

- 1) The probability distribution below is for the random variable  $X$  = number of mice caught in traps during a single night in small apartment building.

$X$	0	1	2	3	4	5
$P(X)$	0.12	0.20	0.31	0.14	0.16	0.07

- a) Describe  $P(X \geq 2)$  in words and find its value.

Probability that 2 or more mice get caught in traps during a single night. . .

$$P(X \geq 2) = P(2) + P(3) + P(4) + P(5) = .68$$

- b) Express the event "trapping at least one mouse" in terms of  $X$  and find its probability.

$$P(X \geq 1) = 1 - P(0) = .88$$

2) Joe the barber charges \$32 for a shave and haircut and \$20 for just a haircut. Based on experience, he determines that the probability that a randomly selected customer comes in for a shave and haircut is 0.85, the rest of his customers come in for just a haircut. Let  $J$  = what Joe charges a randomly-selected customer.

a) Give the probability distribution for  $J$ .

$J$	20	32
$P(J)$	0.15	0.85

b) Find and interpret the mean of  $J$ ,  $\mu_J$ . (SHOW YOUR WORK!)

$$\mu_J = 20(0.15) + 32(0.85) = \$30.20$$

Over the long run, Joe can expect to make \$30.20 per customer

c) Find and interpret the standard deviation of  $J$ ,  $\sigma_J$ . (SHOW YOUR WORK!)

$$\sigma_J = \sqrt{\sum (X_i - \mu_X)^2 p_i}$$

$$\sigma_J = \sqrt{(20 - 30.20)^2 (0.15) + (32 - 30.20)^2 (0.85)} = \$4.28$$

On average, the cost per customer differs or varies from mean \$4.28.